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# TOPICAL REVIEW

# Superconductivity, Mott–Hubbard states, and molecular orbital order in intercalated fullerides

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#### Abstract

This article reviews the current status of chemically doped fullerene superconductors and related compounds, with particular focus on Mott-Hubbard states and the role of molecular orbital degeneracy. Alkaline-earth metal fullerides produce superconductors of several kinds, all of which have states with higher valence than  $(C_{60})^{6-}$ , where the second lowest unoccupied molecular orbital (the LUMO + 1 state) is filled. Alkali-metal-doped fullerides, on the other hand, afford superconductors only at the stoichiometry  $A_3C_{60}$ (A denotes alkali metal) and in basically fcc structures. The metallicity and superconductivity of  $A_3C_{60}$  compounds are destroyed either by reduction of the crystal symmetry or by change in the valence of  $C_{60}$ . This difference is attributed to the narrower bandwidth in the A3C60 system, causing electronic instability in Jahn-Teller insulators and Mott-Hubbard insulators. The latter metal-insulator transition is driven by intercalation of ammonia molecules into  $A_3C_{60}$ -type superconductors. Furthermore, the triple degeneracy of the LUMO state of C<sub>60</sub> plays a crucial role in the metal-insulator transition and in controlling the magnetic structures of insulating states, possibly providing novel properties of degenerate orbitals. The goal of this article is to establish a unifying picture of fullerene intercalation compounds, and to clarify the underlying physics: competing energy scales and orbital properties of molecule-based systems.

(Some figures in this article are in colour only in the electronic version)

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# 1. Introduction: the current status of fullerene superconductors

The development of the Krätchmer-Huffman method of mass production of fullerene molecules [1] in 1990 motivated solid-state fullerene research, as a result of which the superconductivity of  $A_3C_{60}$  fullerides was discovered [2, 3]. (Here, A denotes alkali metal.) Subsequent to the maximum critical temperature  $(T_c)$  of 33 K at ambient pressure being achieved in 1991 [4], C<sub>3</sub>C<sub>60</sub> was found to be superconducting only under high pressure and to show a broad onset at 40 K [5]. These transition temperatures are the second highest among noncuprate superconductors [6]. Figure 1 shows a C<sub>60</sub> molecule and its three molecular orbitals crossing the Fermi energy. The highest occupied molecular orbital (HOMO) is fivefold degenerate, having h<sub>u</sub> symmetry, while the lowest unoccupied molecular orbital (LUMO) and the LUMO + 1 states are both triply degenerate, with  $t_{1u}$  and  $t_{1g}$  symmetry, respectively. To date, the two LUMO levels have been accessed either by chemical doping or the field-effecttransistor technique [7]. Among the approaches tried, chemical intercalation of  $C_{60}$  with metals has produced a particularly rich variety of conducting compounds with carriers introduced in the  $t_{1u}$  and  $t_{1g}$  bands. It is well established that bulk superconductivity is observed both in  $t_{1u}$ and  $t_{1g}$  bands. The highest values of  $T_c$  for the  $t_{1g}$  and  $t_{1u}$  states are 8 and 33 K (40 K at high pressure), respectively.

Table 1 summarizes the characteristics of fullerene superconductors, which are chemically and structurally identified. Not only alkali metals but also alkaline-earth and rare-earth metals are known to afford  $C_{60}$ -based superconductors. For providing a simpler view of fullerene superconductivity, the nominal electron count *n* per  $C_{60}$  molecule (the molecular valence), which is calculated from the ionic crystal model, is quite useful. For example, in the case of  $K_3C_{60}$  [3], the value of *n* is 3. In the case of Ba<sub>4</sub>C<sub>60</sub> [24], *n* is estimated to be 8, since Ba is nominally divalent. Because the two LUMOs ( $t_{1u}$  and  $t_{1g}$  states) of  $C_{60}$  are both triply degenerate (figure 1), the issue of intercalation of  $C_{60}$  with metals is regarded as that of filling two triply degenerate orbitals with electrons. When the valence *n* is smaller than 6, only the  $t_{1u}$  state is filled with electrons. When *n* exceeds 6, the LUMO is fully occupied and the  $t_{1g}$ state is filled. The highest *n* obtained so far is 12, as seen in Ba<sub>6</sub>C<sub>60</sub> and Sr<sub>6</sub>C<sub>60</sub> [22, 29].

From the above point of view, alkali-doped  $C_{60}$  superconductors are classified into one group, namely, the trivalent (n = 3) system, despite the variety and complexity of the materials. Several ammonia-containing compounds, which will be discussed in the following sections, are also included in the n = 3 group, since ammonia molecules are incorporated in a neutral state. Generally speaking, alkaline-earth and rare-earth compounds yield compounds with higher



Figure 1. The molecular structure and electronic energy levels of neutral  $C_{60}$  around the Fermi energy.

	<u>.</u>	Lattice	T (17)	ЪĆ
Compounds	Structure	parameters (A)	$T_c$ (K)	References
	Alkali-	metal-doped C <sub>60</sub>		
Li <sub>3</sub> CsC <sub>60</sub>	fcc	a = 14.080	10.5	[8]
Na <sub>2</sub> KC <sub>60</sub>	fcc	a = 14.122	2.5	[9, 10]
Na <sub>2</sub> RbC <sub>60</sub>	fcc	a = 14.092	3.5	[9, 10]
Na <sub>2</sub> CsC <sub>60</sub>	fcc	a = 14.126	12	[9, 10]
K <sub>3</sub> C <sub>60</sub>	fcc	a = 14.240	19	[3, 10]
$K_x Rb_{3-x} C_{60} \ (0 < x < 3)$	fcc	a = 14.24 - 14.29	19–29	[11]
$K_2CsC_{60}$	fcc	a = 14.292	24	[11]
Rb <sub>3</sub> C <sub>60</sub>	fcc	a = 14.384	29	[12]
Rb <sub>2</sub> CsC <sub>60</sub>	fcc	a = 14.431	31	[11]
RbCs <sub>2</sub> C <sub>60</sub>	fcc	a = 14.555	33	[4]
$Cs_3C_{60}$	bct	a = 12.06, c = 11.43	40 (high P)	[5]
$(NH_3)_4Na_2CsC_{60}$	fcc	a = 14.473	30	[13]
$(NH_3)_x NaK_2C_{60} \ (0.5 < x < 1)$	fcc	a = 14.35 - 14.40	8-13	[14]
$(NH_3)_x NaRb_2C_{60} (0.5 < x < 1)$	fcc	a = 14.50 - 14.53	8.5-17	[14]
(NH <sub>3</sub> )K <sub>3</sub> C <sub>60</sub>	bco	a = 14.971, b = 14.895,	28 (high P),	[15],
		c = 13.678	AFI $(P = 1 \text{ bar})$	[16]
$(NH_3)_x K_3 C_{60} \ (0 < x < 1)$	fcc	a = 14.32	8.5	[17]
$Na_x N_y C_{60}$	fcc	a = 14.204	12	[18]
$Na_x NyC_{60}$	fcc	a = 14.356	15	[19]
	Alkaline-ea	rth-metal-doped C60		
Ca5C60	sc	a = 14.01	8.4	[20]
Sr <sub>4</sub> C <sub>60</sub>	bco		4	[21]
Ba <sub>4</sub> C <sub>60</sub>	bco	a = 11.610, b = 11.234,	6.7	[22, 23]
		c = 10.882		[24]
K3Ba3C60	bcc	a = 11.245	5.6	[25]
$Rb_3Ba_3C_{60}$	bcc	a = 11.338	2.0	[26]
$K_2Ba_4C_{60}$	bcc	a = 11.212	3.6	Present
2 4 00				result
	Rare-eart	h-metal-doped C <sub>60</sub>		
Yb <sub>2.75</sub> C <sub>60</sub>	Orthorhombic	a = 27.87, b = 27.98,	6	[27]
		c = 27.87		
Sm <sub>2.75</sub> C <sub>60</sub>	Orthorhombic	a = 28.17, b = 28.07,	8	[28]
		c = 28.27		

Table 1. Chemically and structurally identified fullerene superconductors

valence. The highest valence that has been identified for a superconducting phase is n = 10, for Ca<sub>5</sub>C<sub>60</sub> [20]. Combination of alkali and alkaline-earth metals produces new compounds with unique valence states. For instance, the valence of K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> [25] is estimated to be n = 9, which had not been achieved in simple binary phases. Yb- or Sm-doped compounds also yield superconductors. According to x-ray photoemission spectroscopy, the Yb ion is divalent in the Yb<sub>2.75</sub>C<sub>60</sub> superconducting phase [27, 30]. Thus, the valence *n* of C<sub>60</sub> is estimated to be 5.5.

A relation between  $T_c$  and the formal valence of  $C_{60}$  is presented in figure 2. First, it should be pointed out that doping with alkali metals produces only trivalent superconductors with the fcc structure. The highest  $T_c$  (33 K) at ambient pressure among the chemical methods is obtained in the alkali-metal-doped compound. Generally, alkaline-earth and rare-earth metals produce compounds with higher valence states. In particular, intercalation of alkaline-



**Figure 2.** The relation between  $T_c$  and the formal valence of  $C_{60}$ , where the highest  $T_c$  for each group is presented. The formal valence is calculated assuming monovalent alkali ions and divalent alkaline-earth and rare-earth ions. For 0 < n < 6, the  $t_{1u}$  band is partially filled, while the  $t_{1g}$  band is partially filled for 6 < n < 12.

earth metal yields superconductors with various valences and crystal structures. However,  $T_c$  for these high-valence materials is substantially lower than those of alkali-metal-doped compounds.

One of the goals of this article is to review the properties of several superconducting compounds with the  $t_{1g}$  conduction band, which is achieved only by intercalation of alkalineearth metals. A number of review articles already published have not paid much attention to the  $t_{1g}$  system [31–34], because of the relatively low values of  $T_c$  and the poor characterization as compared to alkali-metal-doped  $C_{60}$  systems. However, since the chemical and structural criteria for the occurrence of superconductivity in the  $t_{1g}$  band differ considerably from those for the  $t_{1u}$  system, comparison between  $t_{1g}$  and  $t_{1u}$  systems is helpful for obtaining a comprehensive understanding. Thus the first aim of this article is to construct a unifying picture of the electronic states of fullerene superconductors occurring in  $t_{1g}$  and  $t_{1u}$  bands.

Another important characteristic of fullerene superconductors is the empirical relation between  $T_c$  and the interfullerene separation in the trivalent fcc series of superconductors, which is displayed in figure 3. The increase of  $T_c$  with the unit-cell volume (or interfullerene separation) was established early in 1991, and has been believed to be strong evidence for the BCS mechanism of fullerene superconductivity, because the mechanism predicts that  $T_c$ is controlled by the density of states at the Fermi energy  $N(\varepsilon_F)$ , and that enhancement of  $T_c$  or  $N(\varepsilon_F)$  is achieved when the interfullerene transfer energy is reduced by increasing the separation. There have been a number of efforts investigating the effect of pushing the interfullerene separation to a larger magnitude. For instance, for the Cs<sub>x</sub>Rb<sub>3-x</sub>C<sub>60</sub> system it has been shown that a maximum of  $T_c$  in the fcc structure is reached at x = 2, and that  $T_c$  then starts to decrease with increasing separation [35]. Another approach is to intercalate neutral molecules into the A<sub>3</sub>C<sub>60</sub> lattice so that the interfullerene spacing is increased while the valence of C<sub>60</sub> is kept unchanged. In particular, intercalation of neutral ammonia molecules has been extensively investigated and a variety of compounds have been reported on. The highest  $T_c$ achieved taking this direction is 29 K for (NH<sub>3</sub>)<sub>4</sub>Na<sub>2</sub>CsC<sub>60</sub> [13]. However, the ammoniation



**Figure 3.** A plot of  $T_c$  versus volume/molecule for alkali-metal-doped C<sub>60</sub> superconductors in the trivalent state (n = 3). Filled and open circles are data points at ambient and high pressures, respectively.

technique has revealed a new aspect of fullerene intercalation compounds: the Mott–Hubbard transition and the correlation between the orientation/orbital order of  $C_{60}$  molecules and the magnetic structure.

The electron correlation effect has not been apparent in trivalent fullerides, particularly when one pays attention only to superconductors. On the other hands, the importance of electron correlation was indicated experimentally early in 1992, by Auger electron spectroscopy of  $C_{60}$  [36]. Researchers found that the on-ball Coulomb energy U is more than 1 eV, which is considerably larger than the bandwidth of typical fullerites. In fact, the electronic ground state of monovalent fullerides (A1C60 polymer) was found to be a spin density wave (SDW) state, indicating that the electron correlation effect does play a crucial role [37]. In the trivalent superconducting materials  $A_3C_{60}$ , however, Coulomb interaction or electron correlation has been believed to impose only a minor energy scaling, since the band picture and the BCS scheme were very successful. The first evidence for an electron correlation effect in the vicinity of trivalent superconductors was obtained in 1996 for one of the ammoniated trivalent fullerides,  $(NH_3)K_3C_{60}$  [38, 39]. This compound, first synthesized by Rosseinsky and co-workers in 1994 [15], does not superconduct, despite an interfullerene spacing comparable with that of the  $Rb_2CsC_{60}$  superconductor with  $T_c = 31$  K. The crystal structure of  $(NH_3)K_3C_{60}$  is very close to fcc, but has a slight orthorhombic distortion. Electron spin resonance (ESR) studies [38, 39], followed by muon spin rotation ( $\mu$ SR) [40], high-field ESR [41], and nuclear magnetic resonance (NMR) investigations [42], provided unambiguous evidence for an antiferromagnetic insulating ground state for this compound. In other words, the superconductivity of  $K_3C_{60}$  is destroyed by insertion of neutral molecules and replaced by an antiferromagnetic state. The most important point relating to this phenomenon is that the transition between the superconductor and the antiferromagnetic insulator is induced by the lattice symmetry, since there remains an orbital degree of freedom in  $C_{60}$  compounds with nearly cubic structure [42]. This provided a first example of the orbital degree of freedom

playing an important role in molecule-based materials. The second goal of this article is to review the status of the metal-insulator transition and the effect of orbital degeneracy in trivalent fullerides.

In section 2, the synthesis, structure, and properties of  $t_{1g}$  superconductors are presented. In section 3, the electronic properties of compounds with  $t_{1u}$  states—particularly, breakdown of the band picture caused by Jahn–Teller instability—is addressed. Section 5 gives a comparative argument regarding properties of  $t_{1u}$  and  $t_{1g}$  states. In section 4, the Mott–Hubbard transition in ammoniated alkali fullerides is discussed. Section 6 shows that the molecular orientation/orbital order is closely correlated with the magnetic structure in the antiferromagnetic state. Finally, in section 7, a brief summary and perspectives will be given.

#### 2. Barium-doped superconductors in t<sub>1g</sub> states

Kortan and co-workers [20] discovered, in 1992, superconducting materials in the t<sub>1g</sub> state, through intercalation with alkaline-earth metals (Ca, Sr, and Ba). They first reported the superconductivity of  $Ca_5C_{60}$ , with  $T_c = 8$  K. A preliminary structural study suggested that the superconducting phase is fcc-derived simple cubic, but the detailed structure of this phase remains to be established. They subsequently reported the superconductivity of  $Ba_6C_{60}$  and  $Sr_6C_{60}$  [21, 22]. Later, careful experimental examinations proved that the true superconducting phase is body-centred orthorhombic (bco) Ae<sub>4</sub>C<sub>60</sub>. Here Ae denotes Ba or Sr. Baenitz et al [23] were the first to show, in 1995, that the superconducting phase of Ba-doped  $C_{60}$  could be orthorhombic. However, since their sample contained the orthorhombic phase as a minority phase, the phase identification was not necessarily conclusive. In 1999, synthesis of singlephase Ba<sub>4</sub>C<sub>60</sub> presented unambiguous evidence for the superconductivity of the orthorhombic  $Ba_4C_{60}$  phase [24].  $Ba_4C_{60}$  is the first fully identified noncubic superconductor without a fcclike arrangement of  $C_{60}$  molecules. The crystal structure of  $Ba_4C_{60}$  is displayed in figure 4. The structure is similar to the body-centred tetragonal structure of K<sub>4</sub>C<sub>60</sub> and Rb<sub>4</sub>C<sub>60</sub> [43], in which the orientation of the C<sub>60</sub> molecule is disordered. In contrast, the orientation of the molecule is fully ordered in Ba<sub>4</sub>C<sub>60</sub>, resulting in the space group *Immm*. This structure is identical to that of  $Cs_4C_{60}$ , where the increased metal-fullerene interaction due to the large ionic radius causes the full orientational ordering [44]. Although the ionic radius of  $Ba^{2+}$  is almost identical to that of  $K^+$ , the larger Madelung energy due to the larger ionicity induces the contraction of the lattice parameter and, consequently, the full orientational ordering,

The left-hand panel of figure 5 shows the Raman spectra of pristine and Ba-doped  $C_{60}$  compounds [29]. The strongest peak at around 1400 cm<sup>-1</sup> is assigned as a tangential mode,  $A_g(2)$ , of  $C_{60}$  and is known to be a sensitive probe for the charge transfer to the  $C_{60}$  molecule. In the case of alkali metal doping, where full charge transfer is achieved, the Raman shift shows a downshift at a rate of  $\sim 7 \text{ cm}^{-1}$ /charge [45]. The relation between the Raman shift of the  $A_g(2)$  mode and the formal valence is plotted in the right-hand panel of figure 5. The experimental result shows that the Raman shift of  $Ba_3C_{60}$  is almost identical to that of  $K_6C_{60}$ , and increase of the Ba concentration causes a downshift of the  $A_g(2)$  mode at approximately the same rate as in the case of alkali metal doping. This result indicates that the charge transfer from Ba to  $C_{60}$  is also nearly complete (in the first-order approximation). In other words,  $Ba_3C_{60}$ ,  $Ba_4C_{60}$ , and  $Ba_6C_{60}$  should be close to hexavalent, octavalent, and dodecavalent, respectively. Thus  $Ba_4C_{60}$  should have a partially filled  $t_{1g}$  band, while  $Ba_3C_{60}$  and  $Ba_6C_{60}$  have full  $t_{1u}$  and  $t_{1g}$  bands, respectively.

Mixing of alkaline-earth metals and alkali metals produces a new valence state. An example is provided by  $A_3Ba_3C_{60}$  (A = K, Rb, and Cs), which produces a nonavalent state  $(C_{60})^{9-}$  according to simple electron counting [25, 26]. The nominal nonavalent state has not



Figure 4. The crystal structure of superconducting  $Ba_4C_{60}$  viewed from the [001] direction.



**Figure 5.** Left: Raman spectra for pristine and Ba-doped  $C_{60}$  in the region near the pentagonal pinch mode. The highest peak is assigned as the  $A_g(2)$  mode. Right: the Raman shift in wavenumber of the  $A_g(2)$  mode versus the formal valence of  $C_{60}$ . Diamonds and circles correspond to K-doped and Ba-doped  $C_{60}$  compounds respectively. The formal valence of  $C_{60}$  is estimated assuming the ionic crystal model, where complete charge transfer from divalent Ba ions and monovalent K ions to  $C_{60}$  occurs.

been achieved in binary compounds, partly because the reaction of rare-earth elements such as La and Ce, which could be trivalent, has not been successful due to the low vapour pressure. A<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> is synthesized by reaction of alkali metals with preformed Ba<sub>3</sub>C<sub>60</sub>. The crystal structure is identical to those of Ba<sub>6</sub>C<sub>60</sub> and K<sub>6</sub>C<sub>60</sub>, with the space group  $Im\bar{3}$ . The structure of A<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> is the solid solution of these two end compounds. Importantly, this nonavalent phase shows superconductivity with a maximum  $T_c$  of 5.6 K.

Another possible superconducting ternary system is  $K_2Ba_4C_{60}$ . The process of synthesis of this compound is similar to that for  $K_3Ba_3C_{60}$ : excess potassium is intercalated into preformed



**Figure 6.** The temperature dependence of the zero-field-cooled magnetic susceptibility for  $Ba_4C_{60}$  (filled triangles),  $K_3Ba_3C_{60}$  (filled circles), and  $K_2Ba_4C_{60}$  (open circles).

Ba<sub>4</sub>C<sub>60</sub>. Figure 6 shows the temperature dependence of the magnetic susceptibility for Ba<sub>4</sub>C<sub>60</sub>, K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub>, and K<sub>2</sub>Ba<sub>4</sub>C<sub>60</sub>. The superconductivity signal of Ba<sub>4</sub>C<sub>60</sub>, with  $T_c = 6.7$  K, immediately disappears upon doping with K, displaying two onsets of superconductivity. One is at 5.6 K, which is attributable to K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub>. Since Ba<sub>4</sub>C<sub>60</sub> always contains a small amount (a few per cent at most) of stable Ba<sub>3</sub>C<sub>60</sub> as a minority phase, the formation of K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> is inevitable. We observed another onset of a diamagnetic signal at 3.6 K, which should be attributed to K<sub>2</sub>Ba<sub>4</sub>C<sub>60</sub>. The volume fraction of this superconducting phase reaches 14%, indicating that this is a bulk superconductor.

To identify the superconducting phase, a high-resolution x-ray diffraction pattern was recorded at a synchrotron radiation facility, KEK-PF, BL1B, and is shown in figure 7. The structure is again identical to the bcc K<sub>6</sub>C<sub>60</sub> and Ba<sub>6</sub>C<sub>60</sub> ones, with the space group  $Im\bar{3}$  and the lattice parameter a = 11.212 Å. This parameter is in between those of K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> and Ba<sub>6</sub>C<sub>60</sub>, indicating that the compound has an intermediate composition. A Rietveld structural analysis has revealed that the refined chemical composition is K<sub>1.79(1)</sub>Ba<sub>4.20(1)</sub>C<sub>60</sub>. Here, the sum of the K and Ba concentrations was constrained to be 6, to reduce the number of independent parameters. The same analysis on the nominal K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> phase with  $T_c = 5.6$  K, carried out to provide a reference, gave K<sub>2.99(1)</sub>Ba<sub>3.01(1)</sub>C<sub>60</sub>, showing reasonable and systematic variations. The results of the Rietveld analysis of nominal K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> and K<sub>2</sub>Ba<sub>4</sub>C<sub>60</sub> are summarized in table 2. On the basis of the magnetic and structural characterization, we conclude that intercalation of Ba<sub>4</sub>C<sub>60</sub> with K produces another superconducting phase: K<sub>2</sub>Ba<sub>4</sub>C<sub>60</sub> with  $T_c = 3.6$  K. The nominal valence of C<sub>60</sub> in K<sub>2</sub>Ba<sub>4</sub>C<sub>60</sub> is (C<sub>60</sub>)<sup>-10</sup>.

Now, superconductors of several types in the  $t_{1g}$  band are established: octavalent  $Ba_4C_{60}$  and  $Sr_4C_{60}$  (bco), nonavalent  $K_3Ba_3C_{60}$  (bcc), and decavalent ( $K_2Ba_4C_{60}$  (bcc),  $Ca_5C_{60}$  (simple cubic)) fullerides. The occurrence of superconductivity in materials with different band fillings and crystal structures is in sharp contrast with the case for  $t_{1u}$  superconductors which are, in



**Figure 7.** A synchrotron x-ray diffraction pattern for nominal  $K_2Ba_4C_{60}$  for the wavelength of 0.688 81(3) Å. Open circles and solid lines show observed and calculated patterns, respectively. The deviations between these two data sets are displayed at the bottom. Ticks mark the positions of the Bragg reflections. The results of the analysis are summarized in table 2.

principle, restricted to the fcc  $A_3C_{60}$  group. Among these materials, a systematic investigation has been made on the  $A_3Ba_3C_{60}$  system.

 $T_c$  for this system is plotted against the bcc lattice parameter in figure 8.  $T_c$  decreases as a function of lattice parameter, in sharp contrast to the well-known case for A<sub>3</sub>C<sub>60</sub>, where  $T_c$  is an increasing function of the lattice parameter. Measurements of the magnetic susceptibility revealed that the low  $T_c$  compared to those of A<sub>3</sub>C<sub>60</sub> compounds is predominantly attributable to the low density of states at  $\varepsilon_F$ . From magnetic susceptibility experiments, the value of  $N(\varepsilon_F)$  was obtained as 5.7 and 4.1 states  $eV^{-1}/(C_{60} \text{ spin})$  for K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> and Rb<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub>, respectively. These values are considerably lower than that for K<sub>3</sub>C<sub>60</sub>(13 states  $eV^{-1}/(C_{60} \text{ spin})$ ). It is noted that the value of  $N(\varepsilon_F)$  for Rb<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub>, with larger interfullerene spacing, is smaller than that for K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> is ascribed to the reduction of the density of states, in accord with the BCS picture. However, the naïve band picture, in which the density of states decreases with increasing interfullerene distance, does not hold in the A<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> system, in contrast to the case for A<sub>3</sub>C<sub>60</sub> superconductors.

Possible explanations for this unusual behaviour are given by a first-principles band calculation and a detailed structural study. The former made a comparison of the densities



**Figure 8.** A plot of  $T_c$  versus the bcc lattice parameter for the A<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> system with nominal valence n = 9.

Table 2. Results of the Rietveld refinement of the x-ray powder diffraction of  $K_3Ba_3C_{60}$  and  $K_2Ba_4C_{60}$  superconductors.

$K_3Ba_3C_{60}$								
Lattice parameters (Å)	11.2360(1) Im3							
Space group								
<i>R</i> -factors (%) $R_p = 3.05, R_{wp} = 3.14$								
Atomic coordinates and		x	у	z	B (Å <sup>2</sup> )			
thermal parameters								
	C(1)	0.064 4(1)	0.00000	0.3090(1)	0.016(1)			
	C(2)	0.1287(1)	0.1049(2)	0.2718(1)	0.016(1)			
	C(3)	0.063 3(2)	0.205 2(1)	0.2330(2)	0.016(1)			
	Ba <sup>+2</sup>	0.00000	0.500 00	0.2797(2)	0.023(1)			
	$K^{+1}$	0.000 00	0.500 00	0.2797(2)	0.023(1)			
Refined composition K <sub>2.99(1)</sub>				Ba <sub>3.01(1)</sub> C <sub>60</sub>				
		K <sub>2</sub> Ba <sub>4</sub> C <sub>6</sub>	0					
Lattice parameters (Å) 11.2122(1)								
Space group	Im3							
R-factors (%)	$R_p = 2.65, R_{wp} = 3.05$							
Atomic coordinates and		x	у	z	B (Å <sup>2</sup> )			
thermal parameters			-					
	C(1)	0.063 9(1)	0.000 00	0.3097(2)	0.016(1)			
	C(2)	0.1323(1)	0.1033(2)	0.2727(1)	0.016(1)			
	C(3)	0.061 5(2)	0.2068(2)	0.2318(1)	0.016(1)			
	Ba <sup>+2</sup>	0.000 00	0.500 00	0.2808(3)	0.023(1)			
	$K^{+1}$	0.000 00	0.500 00	0.2808(3)	0.023(1)			
Refined composition	$K_{1.79(1)}Ba_{4.20(1)}C_{60}$							

of states at  $\varepsilon_F$  for K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> and Rb<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub>, and showed that, due to the hybridization of Ba and carbon orbitals, the naïve picture is not appropriate in the case of A<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub>. In fact, the calculated densities of states for K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> and Rb<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> are almost identical [46]. The latter experiment revealed that the atomic positions of K and Ba are slightly different, causing a local distortion in the solid-solution structure of A<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub> [47]. Although the ionic radii of K<sup>+</sup> and Ba<sup>2+</sup> are very similar, Rb<sup>+</sup> and Cs<sup>+</sup>, which have larger ionic radii, induce more serious distortion in the structure. This may explain the reduction of  $T_c$  in this system. More investigations are still necessary for a deeper understanding of this system.

As a brief summary of the properties of  $t_{1g}$  superconductors, we can say that doping with alkaline-earth metals often yields  $C_{60}$  superconductors that have a full  $t_{1u}$  conduction band and a partially filled  $t_{1g}$  conduction band. It seems that there are no particular rules for the occurrence of superconductivity. Superconductivity is observed in various crystal structures, such as orthorhombic, bcc, and fcc-derived simple cubic. Also there is no strict regulation of the nominal valence state. Superconductivity seems to be achieved once partial filling of the  $t_{1g}$  band is obtained. The value of  $N(\varepsilon_F)$  for the  $t_{1g}$  system is considerably smaller than that for  $t_{1u}$  superconductors, resulting in the low  $T_c$ , below 8 K. All these situations suggest that the band picture is successful for all the band-filling states in the  $t_{1g}$  system.

## 3. Electronic properties of the t<sub>1u</sub> states

Superconductivity in the  $t_{1u}$  states has been observed in alkali-metal-doped  $C_{60}$  with the composition  $A_3C_{60}$  and in rare-earth-metal-doped  $C_{60}$ ,  $Yb_{2.75}C_{60}$ , and  $Sm_{2.75}C_{60}$ . Since the understanding of the latter system is quite poor at this moment, we will focus our attention on the former system in this section. There are several important features of the  $A_3C_{60}$ -type superconductors:

- (1) n = 3 is the sole electron filling state which yields superconductivity in the alkali-metaldoped systems.
- (2) Superconductivity in the n = 3 state appears exclusively in the fcc and fcc-derived simple cubic structures.
- (3) The band model + BCS picture seems quite successful for the n = 3 superconductors.

The success of both the band model and the BCS picture is of particular importance, since they provided a simple guideline for improving  $T_c$ : if the interfullerene spacing is expanded, the transfer energy or bandwidth becomes smaller. Consequently, the density of states at the Fermi energy  $N(\varepsilon_F)$  is enhanced, causing the improvement of  $T_c$  (figure 3). These situations are well described in the former review articles [31–33].

However, we would like to stress that this band model + BCS picture is valid only for the n = 3 state and fcc structures. It is of particular importance to the BCS-based superconductivity that the normal state is metallic in a manner consistent with the band model, which predicts metallic states for partially filled conduction bands. Nonetheless, the breakdown of the band model is frequently observed in the t<sub>1u</sub> states, in contrast to the case for the t<sub>1g</sub> system. In this section, we describe one example of failures in the band model of C<sub>60</sub> solids.

 $K_4C_{60}$ , a neighbouring compound of superconducting  $K_3C_{60}$ , is known to be an insulating material, in contradiction to the band picture prediction [48–50]. Since the filling of the LUMO is partial (n = 4) in  $K_4C_{60}$ , a metallic state is anticipated in the same way as for  $K_3C_{60}$ . A band structure calculation, taking the tetragonal structure of  $K_4C_{60}$  into account, also predicts a metallic state [51]. Nonetheless, the semiconducting nature of  $K_4C_{60}$  has been consistently observed in experiments of various kinds from the very early stages of solid-state fullerene research [48–50], and the mechanism of the failure of the band calculation for this material, as



**Figure 9.** Possible Jahn–Teller splitting of the triply degenerate LUMO states for  $Na_2C_{60}$  (n = 2) and  $K_4C_{60}$  (n = 4).

well as the absence of superconductivity, is not fully understood. More recently, another important insulating state has been discovered in  $Na_2C_{60}$ . This compound adopts an fcc structure in which two tetrahedral sites are occupied by Na ions, while the octahedral hole is unoccupied [52]. This system is also expected to be metallic and superconducting because of the partial filling of the LUMO band, and also because the structure is almost identical to that of the superconducting phase  $K_3C_{60}$ . Nonetheless,  $Na_2C_{60}$  turns out to be nonsuperconducting, and recent magnetic experiments revealed that it is not even metallic, but semiconducting [53, 54].

A common feature of Na<sub>2</sub>C<sub>60</sub> and K<sub>4</sub>C<sub>60</sub> is that the semiconducting states of both compounds are magnetically inactive (*nonmagnetic* or spin singlet). The nonmagnetic semiconducting states for these two compounds are most probably explained by the Jahn–Teller effect, where spontaneous deformations of high-symmetry molecules induce the splitting of degenerate levels to gain the electronic energy. On removing degeneracy, both even-numbered valence states (n = 2 and 4) become singlet states, resulting in semiconducting solids (figure 9). The Jahn–Teller-type electron–phonon interaction *S* is strong enough in C<sub>60</sub> solids to destroy the band picture for particular valence states. In fact, Jahn–Teller distortions of C<sub>60</sub> molecules have been directly found by structural analysis of single crystals, such as (NH<sub>3</sub>)<sub>8</sub>BaC<sub>60</sub> [55] and [PNN]<sub>3</sub>C<sub>60</sub> (PNN = *bis*(triphenylphosphine)iminium) [56] single crystals with divalent and trivalent C<sub>60</sub>, respectively, both in isolated states. Although electron energy loss spectra of Na<sub>2</sub>C<sub>60</sub> and even-valence C<sub>60</sub> compounds revealed that the nature of the electronic gap is dominated by the on-ball Coulomb repulsion *U*, the nonmagnetic ground states can be understood only when *S* is taken into account [57].

Experimental evidence of the Jahn–Teller distortion was first provided from the infrared conductivity spectra for  $K_4C_{60}$ , exhibiting splitting of the  $T_{1u}$  intramolecular phonon [44]. This splitting could be understood in terms of reduction of molecular symmetry. However, structural confirmations remain to be carried out for the Na<sub>2</sub>C<sub>60</sub> and K<sub>4</sub>C<sub>60</sub> systems, predominantly due to the orientationally disordered structures. Very recently, structural analysis of powder neutron diffraction data uncovered Jahn–Teller distortion of C<sub>60</sub> molecules in Cs<sub>4</sub>C<sub>60</sub>—taking advantage of the fully orientationally ordered structure [58].

### 4. Comparison of t<sub>1u</sub> and t<sub>1g</sub> states

When comparing properties of  $t_{1u}$ - and  $t_{1g}$ -based materials, one may find the following notable differences:

- (1) The value of  $N(\varepsilon_F)$  for the t<sub>1g</sub> band is considerably smaller than those for the t<sub>1u</sub> band.
- (2) Once the  $t_{1g}$  band is partially filled, the metallic state and superconductivity are simultaneously achieved (Ba<sub>4</sub>C<sub>60</sub>, K<sub>3</sub>Ba<sub>3</sub>C<sub>60</sub>, K<sub>2</sub>Ba<sub>4</sub>C<sub>60</sub> and Ca<sub>5</sub>C<sub>60</sub>). However,  $T_c$ , for this group of compounds, is 8 K at maximum.
- (3) In the t<sub>1u</sub> states, the metallic/superconducting states are often destroyed and both nonmagnetic and magnetic (as shown in the following sections) insulating states are observed.

(4) Superconductivity is found exclusively in the trivalent state for the  $t_{1u}$  states, and  $T_c$  reaches more than 30 K.

An important difference between the electronic properties of the  $t_{1u}$  and  $t_{1g}$  states is as regards the stability of the metallic states. It seems that the metallic state is quite stable in the  $t_{1g}$  band, whereas it is often destroyed in the  $t_{1u}$  band. In other words, there are several instabilities against insulating states in the alkali-metal-doped systems, while such instability is absent in Ba-rich systems. This is one of the most fundamental issues relating to the doped fullerides. In particular, isostructural compounds, such as  $Ba_4C_{60}$  and its alkali metal analogue  $A_4C_{60}$ , provide an important opportunity for comparative study, because they are basically isostructural with partially filled  $t_{1g}$  and  $t_{1u}$  bands, respectively.  $Ba_4C_{60}$  is a superconductor with  $T_c = 6.7$  K, while  $K_4C_{60}$ ,  $Rb_4C_{60}$ , and  $Cs_4C_{60}$  are all nonmagnetic insulators. (Strictly speaking, only  $Cs_4C_{60}$  is isostructural with  $Ba_4C_{60}$  [44], and  $K_4C_{60}$  and  $Rb_4C_{60}$  are tetragonal due to the merohedral disordering of the  $C_{60}$  molecules. But this difference does not play an essential role in the electronic states.)

A clue is obtained by a careful examination of the crystal structure shown in figure 4. It was found that there are some very small interatomic distances between barium and carbon [24] in particular, the distance between Ba(2) and C(21) is 2.990(4) Å, which is almost identical to the sum of the ionic radius of Ba<sup>2+</sup> and the van der Waals distance of carbon. This small distance is strongly suggestive of very strong hybridization of Ba(5d) and C(2p) orbitals, which could broaden the bandwidths. The increase of the bandwidth [59] suppresses several instabilities against the insulating states. This speculation is also supported by first-principles band calculations for Ba<sub>6</sub>C<sub>60</sub>, where the hybridization of Ba and C orbitals plays an important role in the band broadening [60, 61]. Also, the experimentally obtained density of states at the Fermi energy in Ba<sub>4</sub>C<sub>60</sub> is significantly smaller than those of alkali-metal-doped C<sub>60</sub> superconductors [24].

Such orbital hybridization implies that the ionic crystal model, which assumes the complete charge transfer from metals to  $C_{60}$ , is not valid any longer in Ba-doped systems. However, considering the almost continuous Raman shift shown in the right-hand panel of figure 5, the model of complete charge transfer works reasonably well, and the hybridization effect is not so dominant. Importantly, such a small hybridization is sufficient for stabilizing the metallic states.

## 5. The Mott–Hubbard transition in the (NH<sub>3</sub>)A<sub>3</sub>C<sub>60</sub> system

A different type of breakdown of the band picture for the  $t_{1u}$  band is seen in a chemical derivative of a trivalent superconductor,  $K_3C_{60}$ . Among the nonsuperconducting compounds,  $(NH_3)K_3C_{60}$  is the most intriguing and informative system, displaying typical characteristics of breakdown of the band picture. Figure 10 shows a schematic representation of the crystal structure of  $K_3C_{60}$  and  $(NH_3)K_3C_{60}$ . A neutral ammonia molecule is inserted in an octahedral site of  $K_3C_{60}$ , causing a slight distortion of the lattice into an orthorhombic form [15].

A variety of experiments have been performed on  $(NH_3)K_3C_{60}$  and it was found that the ground state of  $(NH_3)K_3C_{60}$  is again an insulator, but, in this case, *magnetic*. The first evidence was provided by ESR measurements. The left-hand panel of figure 11 displays ESR spectra at room temperature for an isostructural series of  $(NH_3)K_{3-x}Rb_xC_{60}$  compounds obtained by alloying the alkali metal site [62]. The ESR spectra were found to become broader with increasing Rb concentration. Similar broadening, encountered in ESR spectra for  $A_3C_{60}$  compounds, has been understood in terms of enhanced spin–orbit interaction in Rb ions. The spin susceptibility can be estimated by double integration of the ESR spectra



**Figure 10.** Schematic crystal structures of  $K_3C_{60}$  and  $(NH_3)K_3C_{60}$ . Large and small spheres represent K ions and NH<sub>3</sub> molecules, respectively.  $C_{60}$  molecules, residing at the face-centred positions, are displayed as small dots. Each tetrahedral and octahedral site is occupied by a single K ion.



**Figure 11.** Left: room temperature ESR spectra for  $(NH_3)A_3C_{60}$  compounds at 9 GHz. The increase of the ESR linewidth with the Rb fraction is ascribed to the enhanced spin–orbit interaction in Rb ions. Right: the temperature dependence of the ESR intensity for  $(NH_3)A_3C_{60}$  compounds. The rapid decrease in intensity marked by arrows indicates the occurrence of antiferromagnetic ordering. The weak anomaly at 150 K (shown by the dotted line) is a sign of a structural phase transition associated with the orientational order of  $C_{60}$  and A–NH<sub>3</sub> groups.

in figure 11. The temperature dependence of the ESR intensity (which is proportional to the spin susceptibility in the paramagnetic state) is displayed in the right-hand panel of figure 11. Importantly, the ESR intensity for all four compounds rapidly decreases with temperature, as marked by arrows. This intensity drop is associated with the broadening of the ESR linewidth, indicating that the transition is an antiferromagnetic ordering, by analogy with that in  $A_1C_{60}$  [37]. The subsequently performed  $\mu$ SR [40], high-field ESR [41], and NMR experiments [42] on (NH<sub>3</sub>)K<sub>3</sub>C<sub>60</sub> confirmed that the drop in the ESR signal is ascribable to antiferromagnetic long-range ordering.

In particular, the oscillatory relaxation curve obtained in the  $\mu$ SR experiment provided the first confirmation of antiferromagnetic long-range order in (NH<sub>3</sub>)K<sub>3</sub>C<sub>60</sub>. Prassides *et al* [40] also suggested that the magnetic moment on the C<sub>60</sub> moiety is close to S = 1/2. <sup>13</sup>C



**Figure 12.** <sup>13</sup>C NMR spectra of  $(NH_3)K_3C_{60}$  at various temperatures. The top panel (a) shows the spectra for paramagnetic states. The bottom panel (b) shows a spectrum for an antiferromagnetic state. In (b), the experimental data are shown as open circles and the solid line represents a best fit to a model calculation. The fit is a sum of the intrinsic (dashed curve) and impurity (dotted curve) signals.

NMR spectra and their temperature variation are shown in figure 12 [42]. NMR data include information not only on magnetic but also on rotational states of the C<sub>60</sub>. At 300 K, a single-peaked spectrum is observed, indicative of the rotation of C<sub>60</sub> molecules. The spectral broadening below  $T_S = 150$  K is evidence for freezing of rotation, which will be discussed in the next section. The tremendous spectral broadening at 4.2 K (shown in the bottom panel of figure 12) provided direct evidence for the antiferromagnetic ordering. The low-spin (S = 1/2) state of C<sub>60</sub> molecules was found from careful analyses of the NMR spectra and the temperature dependence of the relaxation rate  $T_1^{-1}$ .

Figure 13 summarizes the Néel temperature  $T_N$  (determined by ESR data) for the (NH<sub>3</sub>)A<sub>3</sub>C<sub>60</sub> system together with  $T_c$  for A<sub>3</sub>C<sub>60</sub> superconductors. This phase diagram clearly shows that the superconductivity in A<sub>3</sub>C<sub>60</sub> is replaced by antiferromagnetic state in the ammoniated systems, and that these two states are close to each other in terms of volume (or interfullerene distance). Proximity of superconductors, organic compounds, and heavy-fermion systems, where the electron correlation effect plays crucial roles not only in the magnetic state but also in the superconducting state. Since the superconductor–antiferromagnet transition is associated with the structural distortion in the case of ammoniated fullerides, the situation is not



Figure 13. The electronic phase diagram of trivalent fullerides. The hatched region shows the orthorhombic insulator phase. SC and AFI denote the superconducting state and antiferromagnetic insulating state, respectively. Open squares and filled circles show the critical temperatures for superconductivity ( $T_c$ ) and antiferromagnetic order ( $T_N$ ), respectively.

straightforward as in the case of other strongly correlated materials. However, the appearance of antiferromagnetic states in the vicinity of the superconductors shown in figure 13 indicates that the electron correlation is very large also in the trivalent states. Furthermore,  $T_N$  reaches 76 K in (NH<sub>3</sub>)KRb<sub>2</sub>C<sub>60</sub>, which is the highest value among molecule-based materials without magnetic elements. Such a high magnetic ordering temperature is another notable aspect of fullerene-based solids.

According to the band calculation, (NH<sub>3</sub>)K<sub>3</sub>C<sub>60</sub> is expected to be metallic regardless of the structural deformation, because of its odd valence n (=3) [63]. Also, since the volume per C<sub>60</sub> is comparable to that for the Rb<sub>2</sub>CsC<sub>60</sub> superconductor with  $T_c = 31$  K, this compound was first anticipated to be superconducting with  $T_c > 30$  K. Hence, the insulating and magnetic state of  $(NH_3)K_3C_{60}$  is quite surprising and, thus, of particular importance. Such magnetic insulators are known as Mott insulators, where the electrons are localized because of the large on-ball Coulomb interaction U between electrons. The key issue is when the electron localization takes place. At first, the metal-insulator transition was believed to take place at low temperatures, presumably at the Néel temperature or at the structural transition temperature, 150 K (which will be described later). This is partly because the spin susceptibility is approximately temperature independent, as shown in figure 11. Since the ammoniated alkali fulleride samples are obtained only in an air-sensitive powder form, direct measurements of conductivity and optical measurements were not carried out on this compound until very recently, although these are very important physical quantities. Kitano and co-workers [64] determined the ac conductivity at 9 GHz for this series of compounds using a cavity perturbation technique. Figure 14 displays the conductivity for several ammoniated fullerides at 250 K.  $K_3C_{60}$  and (NH<sub>3</sub>)<sub>x</sub>NaRb<sub>2</sub>C<sub>60</sub> compounds, which afford fcc structures and become superconducting, show high conductivity values of the order of  $10^2 - 10^3$  S cm<sup>-1</sup>. In sharp contrast, the conductivity of the orthorhombic (NH<sub>3</sub>)K<sub>3-x</sub>Rb<sub>x</sub>C<sub>60</sub> series is 3-4 orders of magnitude smaller than that of the superconducting fcc fullerides. Since the conductivity measurement is made at 250 K, well above  $T_N$  and the structural transition temperature, the low conductivity should be attributed not to these phase transitions, but to the slight distortion in crystal structure from fcc to face-



**Figure 14.** Microwave conductivity at 250 K against volume/ $C_{60}$ . Open and full circles represent cubic and orthorhombic fullerides, respectively. The hatched line shows the Mott limit. The conductivity decreases very slightly with increasing volume/ $C_{60}$  or interfullerene spacing within isostructural compounds. The dramatic reduction of conductivity (the metal–insulator transition) is associated with the structural change from cubic to orthorhombic.



Figure 15. Models of the charge transfer between trivalent molecules with triply degenerate molecular orbitals (a) and without degeneracy (b) at T = 0 K. In the former case, there are three hopping channels, in contrast to the one hopping channel in the latter case.

centred orthorhombic. In other words, this Mott–Hubbard transition is induced by symmetry reduction of the crystal structure.

Here, we should take into account the triple degeneracy of the  $t_{1u}$  molecular orbital, where three electrons are doped. In principle, this degeneracy and high-symmetry fcc structure is crucial to realizing metallic states in fullerides, as was pointed out by Lu [65] and Gunnarsson *et al* [66]. Figure 15 shows an illustration intended to explain the effect of triple degeneracy. In the cubic crystal field, the triple degeneracy is maintained; there are three channels for electron hopping (figure 15(a)). In contrast, when there is a structural distortion, the degeneracy is lifted, so we have only one hopping channel for electrons if one considers the electron transport at T = 0 K (figure 15(b)). This simple consideration indicates that the structural distortion causes band narrowing, which may result in a metal–insulator transition when the bandwidth W is comparable to U. Also, the splitting of the level in figure 15(b) is consistent with the low-spin state (S = 1/2) observed in the  $\mu$ SR and NMR studies of (NH<sub>3</sub>)K<sub>3</sub>C<sub>60</sub>.

Within a band picture, a large distortion is required to induce splitting of the conduction band. However, a recent theory given by Manini and co-workers [63] showed that even a tiny distortion is sufficient for causing the electron localization when the system is on the verge of

the Mott–Hubbard transition. In fact, the *U*-value is believed to be rather large even in  $A_3C_{60}$  superconductors. Several estimations have shown that  $U \sim 1 \text{ eV}$ , the bandwidth  $W \sim 0.5 \text{ eV}$ , and the Jahn–Teller-type electron–phonon interaction  $S \sim 0.2 \text{ eV}$ . These estimates imply that these important energy scales are competing in intercalated fullerides, and that this is the most essential point for various electronic states such as the superconducting, Jahn–Teller insulating, and Mott–Hubbard insulating ones occurring in fullerides [33, 67]. Hence the superconductivity of  $A_3C_{60}$  fullerides is very fragile against valence shift or structural distortion.

# 6. Molecular orbital order in the (NH<sub>3</sub>)A<sub>3</sub>C<sub>60</sub> system

We have shown in the previous section that the orthorhombic  $(NH_3)A_3C_{60}$  system is a Mott– Hubbard insulator with electrons localized on  $C_{60}$  molecules that undergo antiferromagnetic ordering. Another unique aspect to be stressed is the rotational degree of freedom of the  $C_{60}$  molecule. In this section, we will describe how  $C_{60}$  rotation plays a very important and interesting role in controlling the intermolecular magnetic interaction in the  $(NH_3)A_3C_{60}$ system.

Figure 16 summarizes phase transformation sequences for  $C_{60}$ ,  $K_3C_{60}$ , and  $(NH_3)K_3C_{60}$ . The plasticity of undoped  $C_{60}$  is well known: above the fcc–simple cubic structural transition at 260 K,  $C_{60}$  molecules rotate freely. Below 260 K, molecules show a jumping motion between several stable orientations [68, 69]. This is called ratcheting. When temperature is further reduced, a glass transition takes place at 90 K, below which all rotations are frozen in a disordered fashion. In doped fullerides, on the other hand, rotation of  $C_{60}$  molecules is substantially hindered. In particular, when larger cations are introduced, as in  $K_6C_{60}$ , no molecular rotation is observed. For concentrations of smaller cations, such as  $K_3C_{60}$ , there is no free rotation, but ratcheting is allowed at room temperature. Freezing of the ratcheting motion takes place as a continuous crossover around 200 K [70]. Thus the low-temperature state of  $K_3C_{60}$  is orientationally disordered. Despite this disorder, superconductivity does arise in  $K_3C_{60}$  and related compounds, indicating that superconductivity of fullerides is robust against rotational disorder. The structural transition sequence of  $(NH_3)A_3C_{60}$  is very similar to that of  $K_3C_{60}$ , but in contrast to  $K_3C_{60}$  showing orientational disorder, the low-temperature state of  $(NH_3)A_3C_{60}$  is orientationally *ordered*.

Figure 17 shows the expanded diffraction pattern of  $(NH_3)K_3C_{60}$  at 15 and 300 K [71]. Arrowed peaks in the 15 K pattern are forbidden reflections in the *Fmmm* space group at 300 K. All these peaks were successfully indexed as half-integers, indicating that the unit cell is doubled at low temperature with the space group *Fddd*. Figure 18 displays the temperature dependence of the normalized intensity of superlattice peaks. The critical behaviour of the superlattice intensity below  $T_S = 150$  K unambiguously shows the occurrence of the second-order phase transition. It is also noted that the same phase transition is observed at the same temperature of  $T_S = 150$  K in all other  $(NH_3)A_3C_{60}$  compounds. This structural transition has been detected by ESR measurements, as shown in figure 11.

The crystal structure in the low-temperature phase was determined by a Rietveld analysis of the full powder x-ray diffraction pattern [71]. The occurrence of cell doubling was well accounted for by the orientational ordering of K–NH<sub>3</sub> groups, indicating that not only the C<sub>60</sub> but also the K–NH<sub>3</sub> behave as rotors at temperatures higher than  $T_S$ . The low-temperature structure of (NH<sub>3</sub>)K<sub>3</sub>C<sub>60</sub> is displayed in the left-hand panel of figure 19. NH<sub>3</sub>–K groups are aligned in a ferroelectric fashion along the (110) direction. Although the orientational state of C<sub>60</sub> was not determined by the x-ray diffraction study, Margadonna *et al* [72] have succeeded in determining the orientational order of C<sub>60</sub> molecules by means of neutron diffraction and



Figure 16. The sequence of structural and electronic phase transitions in  $C_{60},\ K_3C_{60},\ and \ (NH_3)K_3C_{60}.$ 



Figure 17. Low-angle x-ray powder diffraction profiles of  $(NH_3)K_3C_{60}$  at 300 and 15 K. Superlattice peaks indexed as half-integers appear at low temperature.



Figure 18. The temperature dependence of the normalized intensity of the superlattice reflections indexed as half-integers in figure 17.



Figure 19. Schematic representations of the crystal structure (left) and magnetic structure (right) for  $(NH_3)K_3C_{60}$ . Solid lines indicate octahedra of K ions surrounding  $C_{60}$  molecules.

Rietveld analysis. They found that, associated with the ordering of K–NH<sub>3</sub> groups, the rotation of C<sub>60</sub> is also ordered: ferro-rotationally along the [110] direction and antiferro-rotationally along the [110] direction. The ordering of K–NH<sub>3</sub> groups causes the distortion of the octahedra of K ions that surround C<sub>60</sub> molecules, as shown in the left-hand panel of figure 19. We presume that this distortion induces the noncubic local potentials on C<sub>60</sub>, and, consequently, that the C<sub>60</sub> molecule is orientationally ordered. In the case of K<sub>3</sub>C<sub>60</sub>, on the other hand, the local potential from the undistorted octahedra remains cubic, resulting in orientational disorder of C<sub>60</sub>. The second-order structural transition in (NH<sub>3</sub>)A<sub>3</sub>C<sub>60</sub>, in contrast to the crossover in K<sub>3</sub>C<sub>60</sub>, is ascribed to the cooperative freezing of two rotors (C<sub>60</sub> and the NH<sub>3</sub>–A group).

The dynamical aspect of the structural phase transition was detected from the <sup>13</sup>C NMR spectra (figure 12). The single-peaked spectrum at 300 K, followed by spectral broadening below  $T_S = 150$  K, indicates that the molecular rotation at room temperature is stopped, in a similar manner to the case for undoped C<sub>60</sub> and K<sub>3</sub>C<sub>60</sub>. More importantly, NMR data provide crucial information on magnetic properties. For instance, the huge broadening of <sup>13</sup>C spectra



Figure 20. Orbital and magnetic order in LaMnO<sub>3</sub>, which provides an analogy with the correlation between molecular orientation and magnetic structures in  $(NH_3)K_3C_{60}$ . Clouds and arrows show d orbitals and spins of  $Mn^{3+}$ , respectively.

in figure 12 is one of the most important pieces of evidence for the antiferromagnetic state, as described in the previous section.

Combining spectral analyses of  ${}^{13}$ C,  ${}^{1}$ H, and  ${}^{15}$ N NMR spectra for the antiferromagnetic state, we were able to uniquely determine the magnetic structure from four possible antiferromagnets within a mean-field theory. The spin structure thus obtained is displayed in the right-hand panel of figure 19. In the [110] direction, spins are antiferromagnetically ordered, while in the [110] direction, spins are aligned ferromagnetically. Here we should note that only relative spin orientations are determined and that the absolute direction of the spin cannot be identified, since the measurement was carried out with powder samples.

When the molecular orientational ordering, determined by structural analyses, is taken into account, we find an intriguing correlation between the molecular orientation of  $C_{60}$  and spin structures. When molecules are ferro-rotationally aligned along the [110] direction, the magnetic interaction is antiferromagnetic. On the other hand, when molecules are ordered antiferro-rotationally along [110], the magnetic interaction is ferromagnetic. In other words, figure 19 indicates that molecular orientations control the magnetic interactions. Such structural and magnetic correlations remind us of the analogy with the Kanamori–Goodenough empirical rule for transition metal oxides, where alternating orbitals produce ferromagnetic interactions, while parallel orbitals produce antiferromagnetic interactions [73]. Figure 20 displays a typical example of a transition metal oxide antiferromagneti, LaMnO<sub>3</sub>, where the orbital is ordered at  $T_S = 780$  K, with antiferromagnetic order following at  $T_N = 140$  K. Here we show a (001) basal plane, in which only alternating orbital order, and thus only ferromagnetic interaction, is observed. The correlation between orbital and magnetic order in LaMnO<sub>3</sub> provides a nice analogy with the case of (NH<sub>3</sub>)K<sub>3</sub>C<sub>60</sub>.

In the case of  $C_{60}$ , the molecular orientational order is closely related to the ordering of molecular orbitals, since half-filled  $t_{1u}$  states have an orbital degree of freedom in structures with high symmetry. In fact, the orthorhombicity in  $(NH_3)K_3C_{60}$  is so small that this crystal

is regarded as a quasi-tetragonal structure. Since the molecular orbital is attached to the molecular skeleton, the orientational order of the molecules is regarded as the ordering of molecular orbitals. Tou *et al* [42] pointed out the orbital degree of freedom in  $(NH_3)K_3C_{60}$  and named this ordering 'molecular orbital order'. The important point is that such molecular orbital order controls spin structures.

The effect of molecular orientational/orbital order is not specific to the  $(NH_3)A_3C_{60}$ system, but perhaps provides a new opportunity to investigate intermolecular magnetic interactions in other  $C_{60}$ -based magnets. For instance, several authors have proposed a similar mechanism of magnetic interactions in a  $C_{60}$ -based ferromagnet (TDAE) $C_{60}$  with the Curie temperature at 16 K [74] (where TDAE denotes tetrakisdiaminoethylene). This Curie temperature of 16 K is more than one order of magnitude higher than those for other molecule-based ferromagnets without magnetic elements [75]. A new mechanism has been required to explain this anomalously high  $T_c$ . According to Kawamoto and co-workers [76], an alternating ordering of Jahn–Teller-distorted molecules should produce ferromagnetic ordering of localized spins on  $C_{60}$ . A recent study of the effect of high pressure on  $T_c$  seems to support this model [77]. More importantly, the single-crystal structural analysis at low temperature suggests that there exist alternating molecular rotations in one of the columns of  $C_{60}$  [78]. However, the relation between molecular orientation and magnetic interactions in (TDAE) $C_{60}$ requires more investigation.

## 7. Summary

The current status of superconductivity, Mott–Hubbard transitions, and the role of degenerate molecular orbitals in these phenomena has been reviewed. Although most of the research in this field has focused on the physical properties of the superconductivity in  $A_3C_{60}$  phases, study of low- $T_c$  superconductors as well as of nonsuperconducting compounds is quite useful for obtaining a comprehensive understanding of fullerene intercalation compounds.

Intercalation of  $C_{60}$  with Ba affords several types of superconductor with different valence and crystal structures. Such tolerance in Ba fulleride superconductors is in sharp contrast with the exclusive criteria for superconductivity in alkali-metal-doped  $C_{60}$ .  $T_c$  for Ba-doped systems is much lower than the highest  $T_c$  for  $A_3C_{60}$  superconductors. While superconductivity and the metallic states are quite robust in the  $t_{1g}$  system, they are quite fragile in the  $t_{1u}$  system against symmetry reduction or Fermi energy shift. Such instability in the  $t_{1u}$  system is most probably attributable to the intrinsic character of the  $C_{60}$  molecule, where both the electron– phonon interaction S and the electron–electron interaction U are of the same order as the bandwidth. However, in the Ba-doped systems, such instability against several insulating states is weakened, and metallic but lower- $T_c$  superconducting states are stabilized due to the effect of hybridization between Ba ions and carbon atoms.

We have shown that, in the physics of  $t_{1u}$  states, orbital degeneracy plays various crucial roles, particularly in the metal–insulator transition and insulating states. Regarding the effect of orbital degeneracy, it is noted that reported bulk superconductivity is so far limited to just C<sub>60</sub>-based compounds, strongly indicating that orbital degeneracy is also related to the dominant mechanism of superconductivity. For instance, Suzuki *et al* [79] have shown that the dynamical Jahn–Teller effect is equivalent to the interorbital tunnelling of Cooper pairs, which is reminiscent of the Suhl–Kondo mechanism of superconductivity in fullerides. We wish to stress that the molecular orbital degeneracy of C<sub>60</sub> is quite unique, possibly providing a novel kind of 'orbital physics' in molecular systems which have been extensively investigated as d-or f-electron-based systems. Further investigations not only of insulating but also of metallic states of fullerides are required to establish the physics of the p orbitals in intercalated fullerides.

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